

PSYC 60 – Statistics  
Spring 2012  
Notes #8

## **2-samples, Independent**

*Book: Chapter 14 - t Test For Two Independent Samples*

### **Weighted average**

A student is interested in estimating the average grade in a class. She samples 4 students after class on monday and another 2 students on tuesday. Assume there's no reason students from monday are different than tuesday. How does she combine these two pieces of information in a weighted average?

Monday	Tuesday
<u>Sample</u>	<u>Sample</u>
90	70
85	80
95	
90	
sum=360	sum=150
mean=90	mean=75

Formula:

Principle: ( do / do not ) take the average of the averages  
get the \_\_\_\_\_ for each sample average and \_\_\_\_\_ them  
get the \_\_\_\_\_ for each sample average and \_\_\_\_\_ them  
\_\_\_\_\_ to calculate a new, weighted average

### **Pooled variance (the "weighted average" for variance)**

Using the class grade data above, the student now wishes to estimate grade variance. How does she combine these two pieces of information in a *pooled variance*

Monday	Tuesday
<u>Sample</u>	<u>Sample</u>
SS=50	SS=50
var=16.7	var=50

Pooled variance - an estimate of a population variance based on 2 or more samples, weighted by each sample's size

Formula:

## **2-samples, Independent**

*Book: Chapter 14 - t Test For Two Independent Samples*

*Exclude 14.8 - Point estimates and confidence intervals*

Example: A drug company is trying to determine if their candidate drug decreases blood pressure in gold fish. They administer the drug to 3 gold fish for a year and give a placebo to 4 different gold fish for a year. Does the drug affect blood pressure? (This example is a 2-tailed test, but 2-sample independent tests can be either 1 or 2 tailed)

<u>Drug</u>	<u>Placebo</u>			
80	90	Drug:	mean = 84	SS = 26
85	94	Placebo:	mean = 91	SS = 30
87	87			
	93			

## **Characteristics**

What does it mean that two samples for different conditions (e.g. DRUG versus PLACEBO) could come from the same population?

if the effect of the drug is \_\_\_\_\_  
then, the DRUG & PLACEBO population  
have the same \_\_\_\_\_ & \_\_\_\_\_

the experimenter believes she is  
sampling from different populations, but  
any sample differences are due to

\_\_\_\_\_

## **Degrees of freedom**

For a 2-sample independent t-test, degrees of freedom (df) = \_\_\_\_\_

Review: for 2-sample dependent t-test, df = \_\_\_\_\_

(Optional explanation, will not be tested: One degree of freedom is lost for each calculation of a sum of square (SS) value. Because you calculate SS twice, once for each sample, you lose 2 degrees of freedom.)

### **Standard Error of the difference between means**

Case A: Assume  $\mu = 20$ .  $\sigma_M = 3$ . What is the range of typical sample means you would expect?

Case B: Assume  $\mu = 20$ .  $\sigma_M = 3$ . Each time you draw a sample, you calculate the sample mean and then find how far that sample mean is from a value of 30. What is the range of typical sample mean differences you would expect?

Case C: Assume  $\mu_1 = 20$ .  $\sigma_M = 3$ . As in case B, you find a sample mean. However, you then draw a 2nd sample from a population with  $\mu_2 = 30$  and  $\sigma_M = 3$ . What is the range of typical sample mean differences you would expect?

Formula:

- subscript reflects diff. between samples
- use of pooled variance
- each sample adds to the variance based on how big the sample size is

SE of the sample mean - NOTES #4

how much sample means deviate from the mean of the population

SE of the sample mean difference - NOTES #7

how much sample mean differences deviates from the mean of pop. differences

SE of the difference between sample means - NEW

how much the difference between two sample means deviates from the difference between two population means

## **Distribution of differences in sample means (like a DSM)**

Youtube: <http://www.youtube.com/watch?v=zzeSjTQg20U>

(Prof. Parris. 18:53 - 21:40)

Just as the DSM is built by repeatedly finding sample means, a distribution can be built by repeatedly finding the difference between samples means from two populations

1. Define two populations, A and B
2. Draw a sample from each population and calculate the sample mean of each
3. Subtract to find the difference in sample means
4. Record that value in the distribution of differences in sample means
5. Repeat many times

The standard deviation of this distribution is  
the SE of the difference between sample means

## **Hypothesis test**

All steps of the hypothesis test are the same as 1-sample t-test except for the test statistic

1. State the hypotheses
2. State the alpha value
3. Determine  $t^*$  (remember  $df = \underline{\hspace{2cm}}$ )
4. Calculate test statistic

5. Make a decision. Examples:

- the difference in sample means between drug and placebo is significant
- the mean for drug is significantly lower than the mean for placebo
- the effect of drug is significant

## **Optional shortcut for SE of the difference in sample means: equal n**

If \_\_\_\_\_, it is not necessary to calculate \_\_\_\_\_ to find \_\_\_\_\_

If you forget to use this shortcut, you will still arrive at the correct value for \_\_\_\_\_

Formula: